

# Detecting Fraudsters in Online Auction Using Variations of Neighbor Diversity

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## Abstract

Inflated reputation fraud is a serious problem in online auction. Recent work suggested that neighbor diversity is an effective feature for discerning fraudsters from normal users. However, there exist many different methods to quantify diversity in the literature. This raises the problem of finding the most suitable method to calculate neighbor diversity for detecting fraudsters. We collect four different methods to quantify diversity, and apply them to calculate neighbor diversity. We then use these various neighbor diversities for fraudster detection. Experimental results on a real-world dataset demonstrate that, although these diversities were calculated differently, their performances on fraudster detection are similar. This finding reflects the robustness of neighbor diversity, regardless of how the diversity is calculated.

**Keyword:** online auction, fraudster detection, neighbor diversity, entropy

## 1. Introduction

Online auction websites have gained increasing popularity for the past few years. This lucrative business opportunity has drawn both the legitimate sellers to conduct their business online and the deceitful users to engage in fraudulent transactions. Therefore, online auction websites often provide a recommendation system or a reputation system to assist their users to distinguish legitimate sellers from fraudsters. The reputation system requests the buyer and the seller of a transaction to give each other a rating after their transaction is committed. Then, the reputation system calculates a reputation score of each user based on all the ratings the user received in his/her previous transactions. Intuitively, users with higher reputation scores are more trustworthy, and consequently are more likely to attract sales [1].

Because the reputation score of a user depends on all the ratings the user received in the past, a legitimate user requires time and efforts to accumulate good ratings from other users. In contrast, a fraudster often commits the so-called “inflated reputation fraud” [2] to accumulate good ratings quickly, and cheats the reputation system into giving him/her a high reputation score. The inflated reputation fraud is often achieved by a collusive group of users who conduct fake transactions within the group and provide good ratings to each other. Since online auction users rely on the reputation score to evaluate the trustworthiness of other users, detecting the inflated reputation fraud has become a key task for online auction websites.

In the literature, many methods have been proposed to detect fraudsters with inflated reputation in online auctions. Some of them adopted the concept of network graph to detect fraudsters who rely on their collaborators to boost up their reputations

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[2-6]. With this concept, social network analysis (SNA) has been found as an effective tool to detect fraudsters and their cohesive groups [2, 5, 6]. In our recent work [7], we proposed the concept of neighbor diversity to detect inflated reputation fraud. The neighbor diversity of a user quantifies the diversity of all traders that have transactions with the user. We showed that the neighbor diversity on the number of received ratings outperformed previous works that use  $k$ -core and/or center weight [2, 5, 6].

In [7], Shannon entropy [8] was adopted to quantify the neighbor diversity. However, different ways to define and calculate diversity exist in the literature. This motivates the idea of using various diversity definitions to calculate neighbor diversity for fraudster detection. Specifically, we adopt the four different definitions of diversity from [9] to calculate the neighbor diversity. Our experimental results show, although these diversities are calculated differently, their performances on fraudster detection are similar. This finding reflects the robustness of neighbor diversity, regardless of how the diversity is calculated.

The remaining of this paper is as follows. Section 2 reviews previous works on fraudster detection. Section 3 applies various definitions of diversity to calculate neighbor diversity. Section 4 describes the data collection process. Section 5 presents the experimental settings and discusses the results. Finally, Section 6 concludes this paper.

## 2. Related Work

Detecting fraudsters with inflated reputation is a critical issue for online auction websites. Many methods have been presented in the literature. Some earlier approaches used the properties derived directly from the transaction history. For example, [10] applied the following user-level features to construct a classifier to detect fraudsters: median and standard deviation of the prices of items bought/sold within different periods of time, and the ratio between the number of items bought and the number of transactions. Later, this approach was improved in [3] by incorporating network-level features. The resulted method constructed a Markov Random Field (MRF) model from past transactions among all users, then applied the results of the user-level features to instantiate the observed values of the nodes in the MRF model, and finally used the belief propagation algorithm to compute the probability of being a fraudster for each node. This method was simplified in [4] by initializing the observed values of the nodes in the MRF model to a constant. Later, the belief propagation algorithm in these approaches [3, 4] were substituted with the loopy belief propagation algorithm [11].

In [12], both the transaction-related features (i.e., frequency, price, comment and connectedness in the transaction network) and user-level features (i.e., age and reputation) were applied to investigate the inflated reputation fraud, where a logistic regression model was built to estimate the likelihood of collusion. Instead of limiting to a small set of features, [13] used a wrapper approach to select a subset of suitable features from a large candidate feature pool to build a classifier for fraudster detection.

SNA has gained popularity for developing fraudster detection approaches over the past few years [14-17]. Because the fraudsters rely on their collusive groups to boost up their reputation by committing fake transactions among themselves, the cohesive relationship among them must appear in their transaction network, where a node and an edge in the transaction network represent a user and a transaction, respectively. Common notions of cohesiveness in SNA include component, clique,  $k$ -core, etc. Among them,  $k$ -core was found to be the most effective for fraudster detection because fraudsters often occur in  $k$ -core subgroups with  $k \geq 2$  [2, 6]. Let  $G = (V, E)$  denote the graph for the social network, where  $V$  is the set of nodes and  $E$  is the set of edges. A subgraph  $H = (W, E/W)$  induced by the set  $W \subseteq V$  is a  $k$ -core if the degree of  $v$  is no less than  $k$  for every  $v \in W$ , and  $H$  is the maximum subgraph with this property. To simplify the network, the duplicate edges between two nodes were removed. Notably, a node might belong to more than one  $k$ -core subgraphs, each with a different  $k$  value. The  $k$ -core attribute of a node is the maximum  $k$  values of all the  $k$ -core subgraphs where this node is a member [18, 19].

The problem of using  $k$ -core alone for detecting fraudsters is low precision. Other features such as core/periphery ratio [2], center weight [5, 20],  $n$ -clique,  $k$ -plex, degree and normalized betweenness [6] were used to resolve this problem. However, they reduce the recall.

The concept of diversity has been widely used in many domains, e.g., ecology [21-24] and portfolio management [9, 25, 26]. Recently, the concept of neighbor diversity was developed to improve both precision and recall for fraudster detection [7]. As previously mentioned, fraudsters mostly do businesses with their collaborators to boost up their reputation. Consequently, their collaborators may exhibit similar characteristics, and consequently reduce the neighbor diversity of a fraudster's neighbors on those characteristics. Experimental results shows that the neighbor diversity on the number of received ratings and on the number of cancelled transactions are effective on discerning fraudsters from normal users [7].

### 3. Variants of Neighbor Diversity

#### 3.1. Original Form

To calculate neighbor diversity, we must first choose an attribute (denoted as  $attr$ ). In [7], the number of received ratings or the number of cancelled transactions, is suggested to be the selected attribute. Then, the users are divided into multiples groups based on the selected attribute. Specifically, if the value of the selected attribute of a user is between 0 and 50, then we place the user in the first group; if the value of the selected attribute of a user is between  $50 \times 2^{i-2}$  and  $50 \times 2^{i-1}$ , then we place the user in the  $i$ -th group where  $i > 1$ . Let  $x$  denote a user,  $p_i(x)$  denote the proportion of  $x$ 's neighbors in the  $i$ -th group, and  $n$  denote the total number of classes. Then, the following constraints must hold.

$$0 \leq p_i(x) \leq 1, \text{ for } i = 1 \text{ to } n \quad (1)$$

$$\sum_{i=1}^n p_i(x) = 1 \quad (2)$$

Finally, the neighbor diversity of a user on the attribute  $attr$  is calculated as the group distribution of the user's neighbors using Shannon entropy [8] as follows:

$$D_s^{attr}(x) = - \sum_{i=1}^n p_i(x) \log_2 p_i(x) \quad (3)$$

In the literature, Shannon entropy has been applied to calculate Shannon's diversity index. Please refer to [27] for how Shannon's entropy is used to study diversity theoretically.

#### 3.2. Variants

The notion of diversity is widely used in many different areas. For example, in portfolio management, diversity is used to avoid overly concentrated portfolios. Various diversity constraints were proposed, such as weight upper/lower bound constraint [28],  $L^p$ -norm constraint [29] and entropy constraint [26]. Lin [9] proposed a canonical form of these diversity constraints such that the value of diversity is restricted to the same range for all these different definitions of diversity. Instead of using Shannon entropy to quantify diversity as did in Section 3.1, we can also adopt these canonical forms for calculating neighbor diversity as described next. For problems related to various diversities, please refer to [26, 28-30].

In what follows, we assume the attribute  $attr$  has been chosen, and the distributions of any user  $x$ 's neighbors on the  $attr$

(i.e.,  $p_i(x)$ ) are known. The max weight neighbor diversity on *attr* of  $x$ , denoted as  $D_{max}^{attr}(x)$ , is the maximum of all  $p_i(x)$  for  $i=1$  to  $n$ , as shown below.

$$D_{max}^{attr}(x) = \max_{i=1 \text{ to } n} p_i(x) \quad (4)$$

The min weight neighbor diversity on *attr* of  $x$ , denoted as  $D_{min}^{attr}(x)$ , is calculated using the minimum of all  $p_i(x)$  for  $i=1$  to  $n$ , as shown below.

$$D_{min}^{attr}(x) = 1 + (1 - n) \min_{i=1 \text{ to } n} p_i(x) \quad (5)$$

The Canonical  $L^p$ -norm neighbor diversity on *attr* of  $x$ , denoted as  $D_{pow}^{attr}(x)$ , is similar to the  $L^p$ -norm except the outer exponent is  $\frac{1}{pow-1}$  instead of  $\frac{1}{pow}$ , as shown below.

$$D_{pow}^{attr}(x) = \left( \sum_{i=1}^n |p_i(x)|^{pow} \right)^{\frac{1}{pow-1}} \quad (6)$$

For the value of *pow*, the cases of  $pow = 2$  and  $3$  are commonly used [9]. Hence, we consider only  $D_2^{attr}(x)$  and  $D_3^{attr}(x)$  in this study.

The canonical Shannon entropy neighbor diversity on *attr* of  $x$ , denoted as  $D_{cs}^{attr}(x)$ , is the reciprocal of the natural exponential function of Shannon entropy, as shown below.

$$D_{cs}^{attr}(x) = e^{-D_S^{attr}(x)} = e^{-\sum_{i=1}^n p_i(x) \log_2 p_i(x)} \quad (7)$$

Notably, as proved in [9], the ranges of the neighbor diversity defined in equations (4) to (6) are all the same, i.e.,  $[\frac{1}{n}, 1]$ . In Eq.(7), we use  $\log_2$  instead of the natural logarithm such that  $D_{cs}^{attr}(x)$  can be easily calculated from  $D_S^{attr}(x)$ . For a theoretical comparison of these diversity equations, please refer to [9].

#### 4. Data Collection and Dataset Preparation

In the study, we collected a dataset from Ruten ([www.ruten.com.tw](http://www.ruten.com.tw)), which is one of the largest online auction websites in Taiwan [31]. Similar to previous works [5-7], the dataset is grown from a list of suspended users, and then conducted a level-wise expansion to include more users. The main reason of choosing Ruten in this study is that Ruten regularly releases a list of suspended users and their reasons of suspension. Notably, a suspended user is not necessarily a fraudster. For example, a user who is suspended by Ruten due to selling cigarettes or alcohol, is not considered as a fraudster in this study. We collected 9,168 suspended users from Ruten during July 2013, manually checked their reasons of suspension to look for fraudsters, and finally, identified 932 out of the 9,168 users as fraudsters. However, the status of one of the 932 users was changed back to normal during October 2013. Therefore, these 932 users, denoted as  $L_1$  users, consist of 931 fraudsters and 1 non-fraudster.

Then, we extended from the  $L_1$  users to find more users by collecting all users who have given a rating to or received a rating from any  $L_1$  user. In this step, 3,475 new users, denoted as  $L_2$  users, were collected, and among them, 149 accounts were classified as fraudsters. Similarly, we further extended from  $L_2$  users to find more users by collecting all users who have given a rating to or received a rating from any  $L_2$  user. In this step, 233, 169 new users, denoted as  $L_3$  users, were collected. Notably,

while collecting the  $L_1$ ,  $L_2$  and  $L_3$  users, we also stored the number of received ratings and the number of cancelled transactions for each user.

In order to calculate the SNA-related features (e.g.,  $k$ -core and center weight) for all users, a social network of all  $L_1$ ,  $L_2$  and  $L_3$  users was built, where each node represents a user and each link represents a rating from one user to another user. To simplify our social network, duplicate links are removed. The resulting social network contains 237,576 ( $=932 + 3,475 + 233,169$ ) nodes and 348,259 links. Notably, the ratings that occurred after 31 July 2013 were not included in the social network.

After the social network was constructed, we calculated  $k$ -core and center weight for each node in the social network, as presented in Section 2. Finally, the neighbor diversity for each  $L_1$  or  $L_2$  user is calculated, as described in Section 3. Notably, the  $L_3$  users are only used to provide a complete view of the  $L_2$  accounts' neighbors. Thus, the final dataset contains only the  $L_1$  and  $L_2$  users, where 1,080 ( $= 931+149$ ) are fraudsters and 3,327 ( $= 1 + 3,475 - 149$ ) are non-fraudsters.

For each user in the dataset, the following attributes are available: the number of received ratings, the number of cancelled transactions,  $k$ -core, center weight, neighbor diversity (i.e.,  $D_s^{attr}$ ) and its variants (i.e.,  $D_{max}^{attr}$ ,  $D_{min}^{attr}$ ,  $D_2^{attr}$ ,  $D_3^{attr}$ , and  $D_{cs}^{attr}$ ). The same dataset without the variants of neighbor diversity was also used in [7]. For the selected attribute  $attr$  in neighbor diversity and its variants, we use the number of received ratings and the number of cancelled transactions because they achieved the best performance in [7]. The resulting attributes are denoted as  $D_s^r$ ,  $D_{max}^r$ ,  $D_{min}^r$ ,  $D_2^r$ ,  $D_3^r$  and  $D_{cs}^r$  for various types of neighbor diversity on the number of received ratings, and as  $D_s^c$ ,  $D_{max}^c$ ,  $D_{min}^c$ ,  $D_2^c$ ,  $D_3^c$ , and  $D_{cs}^c$  for various types of neighbor diversity on the number of cancelled transactions.

## 5. Experimental Results

Because previous works suggest using  $k$ -core and center weight (CW for short) for fraudster detection [5], in the experimental study, we used  $k$ -core, CW and one of the various types of neighbor diversity to build a classifier and compared their performance. Three classification algorithms (J48 decision tree, Neural Networks (NN), and Support Vector Machine (SVM)) from Weka [32] were used to perform 10-fold cross-validation, and the results are shown in Tables 1 to 6.

Tables 1, 2 and 3 show the results of using various types of neighbor diversity on the number of received ratings, where the best result of each classification algorithm is shown in bold. Notably, we also show the results of using only  $k$ -core and CW in these tables to reflect the impact of adding neighbor diversity. With the addition of neighbor diversity, accuracy, recall and  $F_1$ -measure are all improved, although the precision is reduced. Overall, the performance of adding any neighbor diversity is similar, although the performance of adding  $D_{max}^r$  or  $D_{min}^r$  sometimes achieves a small recall (shown in italic in Tables 1, 2, and 3) when using different classification algorithms.

Table 1 J48 Performance of using  $k$ -core and CW with or without  $D^r$

Input	Accuracy (%)	Recall	Precision	$F_1$ -measure
$k$ -core & CW	82.9816	0.5000	0.7200	0.5902
$k$ -core & CW & $D_s^r$	85.8180	0.8731	0.6590	0.7511
$k$ -core & CW & $D_{max}^r$	85.8861	0.8731	0.6604	0.7520
$k$ -core & CW & $D_{min}^r$	84.1162	0.8278	0.6349	0.7186
$k$ -core & CW & $D_2^r$	86.1130	0.8685	0.6662	0.7540
$k$ -core & CW & $D_3^r$	86.2038	0.8704	0.6676	0.7556
$k$ -core & CW & $D_{cs}^r$	85.8180	0.8741	0.6588	0.7513

Table 2 Neural Network performance of using k-core and CW with or without D<sup>r</sup>

Input	Accuracy (%)	Recall	Precision	F1-measure
<i>k</i> -core & CW	79.6006	0.5167	0.5968	0.5539
<i>k</i> -core & CW & $D_5^r$	83.7758	0.7787	0.6386	0.7017
<i>k</i> -core & CW & $D_{max}^r$	84.1616	0.8083	0.6400	0.7144
<i>k</i> -core & CW & $D_{min}^r$	82.3916	0.6620	0.6350	0.6482
<i>k</i> -core & CW & $D_2^r$	83.9120	0.7981	0.6371	0.7086
<i>k</i> -core & CW & $D_3^r$	83.9573	0.8028	0.6370	0.7104
<i>k</i> -core & CW & $D_{cs}^r$	83.8212	0.7843	0.6383	0.7038

Table 3 Support Vector Machine performance of using k-core and CW with or without D<sup>r</sup>

Input	Accuracy (%)	Recall	Precision	F <sub>1</sub> -measure
<i>k</i> -core & CW	82.9362	0.4917	0.7234	0.5855
<i>k</i> -core & CW & $D_5^r$	84.4112	0.7685	0.6551	0.7073
<i>k</i> -core & CW & $D_{max}^r$	83.0043	0.6835	0.6428	0.6625
<i>k</i> -core & CW & $D_{min}^r$	83.4581	0.7630	0.6353	0.6933
<i>k</i> -core & CW & $D_2^r$	83.2539	0.7370	0.6368	0.6833
<i>k</i> -core & CW & $D_3^r$	83.2993	0.7398	0.6372	0.6847
<i>k</i> -core & CW & $D_{cs}^r$	83.0951	0.7426	0.6320	0.6828

Tables 4, 5 and 6 show the results of using various types of neighbor diversity on the number of cancelled transactions. All types of neighbor diversity achieved similar results, and the choice of classification algorithms play a crucial role on their performance. For example, Table 4 shows that the J48 performance is similar in precision with or without using the neighbor diversity on the number of cancelled transactions, and achieves better recall with any neighbor diversity (i.e., comparing row 1 against rows 2 to 7 in Table 4). SVM also has similar results (see Table 6). With neural network (see Table 5), the addition of any neighbor diversity greatly improves the recall but only slightly reduces the precision.

Table 4 J48 Performance of using k-core and CW with or without D<sup>c</sup>

Input	Accuracy (%)	Recall	Precision	F <sub>1</sub> -measure
<i>k</i> -core & CW	82.9816	0.5000	0.7200	0.5902
<i>k</i> -core & CW & $D_5^c$	84.0708	0.5870	0.7124	0.6437
<i>k</i> -core & CW & $D_{max}^c$	84.0481	0.5861	0.7120	0.6430
<i>k</i> -core & CW & $D_{min}^c$	84.0254	0.5907	0.7089	0.6444
<i>k</i> -core & CW & $D_2^c$	84.0481	0.5861	0.7120	0.6430
<i>k</i> -core & CW & $D_3^c$	84.0481	0.5861	0.7120	0.6430
<i>k</i> -core & CW & $D_{cs}^c$	83.9800	0.5861	0.7096	0.6420

Table 5 Neural Network performance of using k-core and CW with or without D<sup>c</sup>

Input	Accuracy (%)	Recall	Precision	F <sub>1</sub> -measure
<i>k</i> -core & CW	79.6006	0.5167	0.5968	0.5539
<i>k</i> -core & CW & $D_5^c$	81.5975	0.8750	0.5830	0.6997
<i>k</i> -core & CW & $D_{max}^c$	81.8698	0.8815	0.5866	0.7044
<i>k</i> -core & CW & $D_{min}^c$	82.1194	0.9130	0.5869	0.7145
<i>k</i> -core & CW & $D_2^c$	81.8698	0.8833	0.5864	0.7048
<i>k</i> -core & CW & $D_3^c$	81.8698	0.8815	0.5866	0.7044
<i>k</i> -core & CW & $D_{cs}^c$	81.8924	0.9019	0.5846	0.7094

Table 6 Support Vector Machine performance of using k-core and CW with or without  $D^c$ 

Input	Accuracy (%)	Recall	Precision	$F_1$ -measure
$k$ -core & CW	82.9362	0.4917	0.7234	0.5855
$k$ -core & CW & $D_5^c$	83.1178	0.5389	0.7029	0.6101
$k$ -core & CW & $D_{max}^c$	82.6866	0.5333	0.6898	0.6016
$k$ -core & CW & $D_{min}^c$	83.2312	0.6241	0.6693	0.6459
$k$ -core & CW & $D_2^c$	82.7547	0.5352	0.6914	0.6033
$k$ -core & CW & $D_3^c$	82.7093	0.5333	0.6906	0.6019
$k$ -core & CW & $D_{cs}^c$	82.8909	0.5343	0.6969	0.6048

## 6. Conclusions

Various ways to quantify diversity exist in the literature [9, 22]. In this work, we apply the diversity of the neighbors of each trader for detecting fraudsters in online auction. Specifically, we use various methods to calculate diversity, and study whether these methods cause significant difference on the classification performance of fraudster detection. Our experimental results show that, using the same classification algorithm, the addition of a neighbor diversity attribute always improves the recall and  $F_1$ -measure. The accuracy is almost always improved, except in the case of adding  $D_{max}^c$  to  $k$ -core & CW in Table 6. Among the various ways to calculate neighbor diversity, they all achieve similar performance, and no one is consistently better than the others.

The performance results also depend on the classification algorithm used. With J48 and SVM, the recall is better with the addition of  $D^r$  than with the addition of  $D^c$ . With neural network, the precision is better with the addition of  $D^r$  than with the addition of  $D^c$ . However, with each of the three classification algorithms, the accuracy is better with the addition of  $D^r$  than with the addition of  $D^c$ . Overall, any form of neighbor diversity on the number of received ratings (see Tables 1, 2 and 3) achieves better accuracy than its corresponding neighbor diversity on the number of cancelled transactions (see Tables 4, 5 and 6).

The original definition of neighbor diversity only considers the direct neighbors, but the relationship among a collusive group may go beyond the direct neighbors. Thus, extending the idea of neighbor diversity to indirect neighbors could be helpful to spot the intrinsic structure of a collusive group. This is left as a possible direction for future work.

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## List of Symbols and Nomenclature

SNA	Social network analysis
J48	Classification tree J48 algorithm
NN	Neural network algorithm
SVM	Support vector machine
CW	Center weight
$D_s^r$	The neighbor diversity on the number of received ratings based on Shannon entropy
$D_{max}^r$	The neighbor diversity on the number of received ratings based on max weight diversity
$D_{min}^r$	The neighbor diversity on the number of received ratings based on min weight diversity
$D_2^r$	The neighbor diversity on the number of received ratings based on canonical $L^p$ -norm diversity with the value of $pow=2$
$D_3^r$	The neighbor diversity on the number of received ratings based on canonical $L^p$ -norm diversity with the value of $pow=3$
$D_{cs}^r$	The neighbor diversity on the number of received ratings based on canonical Shannon entropy
$D_s^c$	The neighbor diversity on the number of cancelled transactions based on Shannon entropy
$D_{max}^c$	The neighbor diversity on the number of cancelled transactions based on max weight diversity
$D_{min}^c$	The neighbor diversity on the number of cancelled transactions based on min weight diversity
$D_2^c$	The neighbor diversity on the number of cancelled transactions based on canonical $L^p$ -norm diversity with the value of $pow=2$
$D_3^c$	The neighbor diversity on the number of cancelled transactions based on canonical $L^p$ -norm diversity with the value of $pow=3$
$D_{cs}^c$	The neighbor diversity on the number of cancelled transactions based on canonical Shannon entropy